

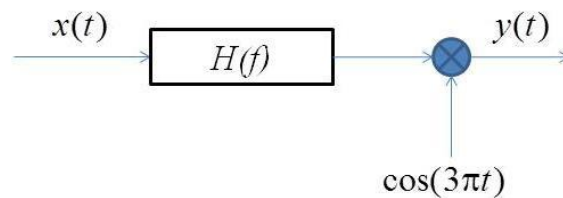
Exam of Digital Communications

a.a. 2015-2016

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Exercise #1

Let $y(t)$ be the output of the following system,

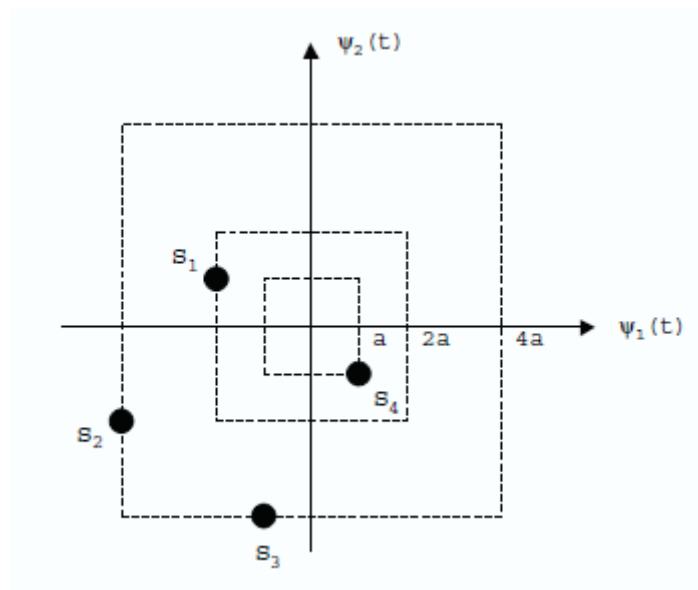


when the input $x(t)=\text{sinc}(t)$ and $H(f)=(1/2)\text{rect}(f/2)$

- (a) Is the signal $y(t)$ narrowband or wideband? Justify your answer.
- (b) Find the complex baseband equivalent of $y(t)$ and sketch its spectrum.
- (a) Give an expression for the Hilbert transform of $y(t)$.

Exercise #2

A digital communication system is designed using bandpass QPSK modulation with Gray mapping. Due to a DC offset and phase error in the modulator, the constellation is translated and rotated as shown in the figure below.



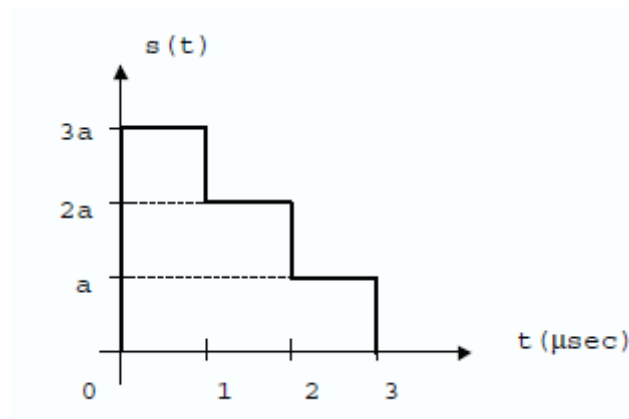
- (a) Compute the average energy of the signals and sketch carefully the decision regions.
- (b) Find the probability of a bit error P_b of this system and compare it with the bit error rate of a conventional QPSK with the same energy per bit E_b (i.e., indicate what is the increase in E_b/N_0 that is needed to achieve the same performance in terms of bit error rate).
- (c) If a demodulator for conventional QPSK is employed, what is the resulting value of P_b ?

Exercise #3

A message signal $m(t)$ is transmitted by binary PCM. Let the signal to-quantization noise (SQNR) required be at least 47 dB. Determine the minimum number of bit required to encode each sample, assuming that $m(t)$ is sinusoidal. With this value of quantization levels, determine the SQNR.

Exercise #4

The pulse waveform shown below is used for binary communication with on-off keying.



- Determine the value of “a” in terms of average energy per bit E_b
- Sketch the impulse response of the filter matched to $s(t)$
- Draw a block diagram of the optimum receiver
- What is the bit rate R_b ? If we want bit rate R_b of 1Mbps using the same shape of the pulse but with a M-PAM modulation, what is the minimum value of M that is required?
- What is the minimum bandwidth that is required for ISI free transmission? Is the bandwidth requirement different in the two considered cases (M-PAM and on-off keying modulation)?

Exercise #5

A new RF technology produces a 5 dB improvement in SNR at the receiver. Discuss how this can be used to enhance performance. Provide some examples.